Analysis of polarization offsets observed for temperature-graded ferroelectric materials

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A R T I C L E   I N F O

Article history:
Received 25 September 2015
Received in revised form 8 February 2016
Accepted 21 February 2016
Available online 24 February 2016
Communicated by R. Wu

Keywords:
Ferroelectric material
Temperature gradient
Polarization offset

A B S T R A C T

A transverse Ising model in the framework of the mean field approximation is developed to analyze the polarization offsets phenomena in temperature-graded ferroelectric materials. A function of two-spin exchange interaction strength has been introduced to describe the ferroelectric distortion due to the distribution of temperature gradients in materials. Comparisons of the computational results with the experimental data reveal some fundamental factors in the formation of polarization offsets. It is shown that ferroelectric distortion has influenced much on polarization offsets in temperature-graded ferroelectric materials. When quantum fluctuation effect as well as ferroelectric distortion is considered, we have successfully reproduced the experimental observations qualitatively, especially for the indistinguishable polarization offsets from the background at small temperature gradients, which were not successfully reproduced in prior theoretical studies.

The ferroelectric material with polarization gradients normal to the growth surface readily form when gradients in temperature, strain, or composition are coupled to the polarization vector in ferroelectric materials. Because of their unconventional ferroelectric properties, they present dramatic hysteresis loop offsets, transcapitor behavior, enormous pyroelectric responses, and other exotic phenomenon [1–20], which have attracted a lot of attention during these years.

A series of investigations were carried out to interpret the origin of the aberrant hysteric behavior persist [1–6]. It was experimentally shown that both “up” and “down” hysteresis offsets can be observed from (Ba0.75Sr0.25)TiO3 bulk ceramics [1]. In this ground-breaking experiment a temperature gradient was established along the polarization direction and yielded highly nonlinear polarization offsets for temperatures near the Curie point. Based on the data retrieved from this experiment, a phenomenological approach was subsequently developed to reproduce the experimental observations [2]. The results were in excellent quantitative agreement with the experiment except the data for small temperature gradients. The experimentally determined charge offsets are indistinguishable from the background variation with small temperature difference between two heat sinks [1], while the theoretical results are quite distinguishable [2]. Also with the available experimental data, a microscopic insight was recently put into the polarization response in this temperature-graded alloy through an accurate first-principle-based computational approach [19]. The maximum value of polarization offset was successfully reproduced, but more detailed comparison was not carried out due to the structural and dimensional differences between the samples used in computations and experiment.

These works have (1) discussed the possible “origin” leading to hysteresis offsets, (2) explored the fundamental understanding of some exotic properties, (3) demonstrated the potential applications of temperature-graded ferroelectrics as well as some possible ways to tailor them. However, despite all these exciting developments, our understanding of polarization-graded ferroelectrics is still limited. The origin of such polarization offsets is still very much controversial. The indistinguishable charge offsets for small temperature gradients still cannot be reproduced and interpreted theoretically.

The aims of this paper are (1) to gain a fundamental microscopic understanding of polarization offsets for temperature-graded ferroelectrics through a developed transverse Ising model, (2) to theoretically reproduce and interpret the behavior of charge offsets at small temperature gradients in the experiment.

Specifically, due to the structure and dimension of the samples in experiment [1] cannot be accurately reproduced in our model, only qualitative comparisons will be made with the experimental results and other theoretical computations.

The model used to describe the material is illustrated in Fig. 1. It is supposed that $3 \times 10^6$ pseudo-spin layers ($N = 3 \times 10^6$) are contained in the film. The ferroelectric material is imposed a tem-
According to Eq. (2), the tunneling frequency $\Omega_m$ of the $m$th layer will increase linearly from $\Omega_{T_0}$ to $(g+1)\Omega_{T_0}$ when the temperature decreases from $T_0$ to 0 K. Thus, the tunneling frequency $\Omega_m$ represents the contribution of the quantum fluctuation.

Zhang et al. [22] have given a qualitative analysis for equation (2). For BaTiO₃, an eight-site potential exists around the Ti ion. The height $h$ of the potential barrier is finite. When $k_BT_i$ is higher than the height $h$, the tunneling effect does not exist, which means $\Omega_m = 0$. For low temperature with $k_BT_i < h$, the tunneling effect exists, implying $\Omega_m > 0$.

Since the quantum fluctuation effects are considered by Eq. (2) in this paper, its physical implication may restrict our calculations to that kinds of ferroelectric with the one order–disorder phase transition and tunneling vibrational mode (small ions such as protons), but the conclusions we draw should have the generality.

It is well known that objects expand when heated and contract when cooled. When temperature gradients are established, due to the nonuniform temperature distribution, some parts inside the sample may expand heavily, some parts may expand thinly, and some parts even contract where temperatures are very low. Thus, the deformations inside are not synchronous, and the ferroelectric distortions will certainly happen.

However, the ferroelectric distortions can modify the interaction strength $J$ and the dipolar moment $\mu$ [22,23]. As it is quite difficult to accurately model the combined electromechanical setup without introducing a number of adjustable free parameters, we suppose the dipolar moment $\mu$ is constant. A function of strength $J$ was introduced to generally describe the ferroelectric distortions in the sample [22,23].

$$J(m) = J_0[1 + F_2P_m^2 + F_4P_m^4 + F_6P_m^6 + \ldots]$$

where $m$ is the sequence number of the pseudo-spin layers. $F_n (n = 2, 4, 6, \ldots)$ are the coefficients to describe the contribution of the ferroelectric distortion. When ferroelectrics are clamped, $F_n = 0$. In free ferroelectrics, $F_2$ will deviate from zero because of the modification of the polarization, which were taken to be some constants in Ref. [22].

In the experiment, the sample was clamped to keep good contact with the heat sinks. According to Ref. [22], $F_2$ should taken to be zero. But when considering the nonuniform temperature distribution inside the films, the nonsynchronous deformations will certainly happen even in the clamped boundary condition. In this case, the consideration of the statistical distributions with temperatures with respect to these coefficients should be realistic and significant. Hence, we modify the function for strength $J$ to the following form,

$$J(m) = J_0[1 + F_2e^{-A}P_m^2 + F_4e^{-B}P_m^4 + F_6e^{-C}P_m^6]$$

$$A = \frac{J_0(1 + F_2P_m^2)}{K_BT}$$

$$B = \frac{J_0(1 + F_2P_m^2)}{K_BT}$$

$$C = \frac{J_0(1 + F_2P_m^2)}{K_BT}$$

The terms higher than the sixth order in the interaction expression are neglected and we take $F_2 = 1.0 \text{ m}^2/\text{e}^2$, $F_4 = 10 \text{ m}^4/\text{e}^4$, $F_6 = 10 \text{ m}^6/\text{e}^6$ as representatives in calculations.

The distribution of temperature gradient in temperature-graded ferroelectrics is very complicated, which is influenced by many factors, such as, the sample thickness, heat-flux density, and thermal-conductivity coefficient etc. [4]. The nonequilibrium molecular dynamics analogous to the experimental method was previously utilized to simulate this thermal transport property, in this case the temperature varies linearly along the sample [19]. Hence a simple uniform temperature gradient is supposed in our calculations, which was adopted in many theoretical works [7–9]. Parameter $a$
is introduced to reflect the uniform temperature gradient. Numerically, it is the temperature ratio of the $N$th layer (bottom layer) temperature $T_N$ and the first layer (top layer) temperature $T_1$, that is,

$$a = T_N / T_1$$

(5)

It is worth noting that the temperature gradients are established by changing the temperature of one of the heat sinks, while the latter is kept fixed, which is the case as well as the works in Ref. [1,2,19]. We fix $T_1 = 280$ K in the following calculations.

In order to phenomenologically describe and explain the polarization offsets in temperature-graded ferroelectric materials, it is convenient to rescale the variables into dimensionless forms. We take $\Omega_0 / J_0 = 1.2$ and $J_0 / (K_B T_0) = 0.1$ as representatives, this particular choice does not affect the generality of the conclusions.

The spontaneous polarizations along the $z$ direction as a function of sequence number $m$ are plotted in Fig. 2. The top panel shows the temperature profile along the $z$ axis, and the bottom panel shows the polarization distribution associated with this temperature profile. We take $a = 0.857$ in the calculation, that is, $\Delta T = 40$ K. Considering the thickness of the sample ($N = 3 \times 10^6$), the temperature gradient is about $\sim 10^4$ K/m, which keeps the same order in the following calculations. The impact of quantum fluctuation is not considered in this figure. It is shown that our results are analogous to the results according to the nonequilibrium molecular dynamics method [19]. The linear temperature difference leads to an almost linear polarization distribution besides at several larger number layers. This result comes out from the competition between the temperature gradient and the interaction couplings strength. Although the last layer has the lowest temperature leading to a larger polarization, the pseudo-spin in the inner layer has a larger coordinate number (six in our case, the coordinate number in the thirtieth layer is five) and a larger in-dimension. Due to the strong and close interactions between those large number layers and the last one, the weak polarizations extend some depth into inner layers. Finally, this competition leads to the largest polarization in some inner layer.

The impact of the quantum fluctuation is considered on a uniform ferroelectric material in Fig. 3. The average polarization is plotted as a function of temperature. It is shown that the quantum fluctuation influences much in polarization, especially when the temperature is not very high. Hence, in following investigation, when temperature-graded materials are concerned, the distribution of quantum fluctuation is inhomogeneous, whose effects will be more obvious in low temperature region. At the same time we can see that the quantum effects do not affect the order of the transition, but do reduce the transition temperatures, which have qualitative agreement with the experimental data in Ref. [1] and the theoretical results in Ref. [9,21].

To eliminate contributions of the boundary conditions and heat sinks, we focus on the region between the $(1 \times 10^6)$th and the $(2 \times 10^6)$th layers of the material (the region shown between the two vertical lines in Fig. 2). We will refer to the leftmost and rightmost boundaries of this region as the two sinks, and the difference in temperature between the two sinks is $\Delta T = T_{1,10^6} - T_{2,10^6}$. Then calculate the polarization offset along the $z$-axis between the two sinks as Ref. [19] $\Delta P_y^{\text{offset}} = P_y(1 \times 10^6) - P_y(2 \times 10^6)$.

In Fig. 4 polarization offset is plotted as a function of temperature difference when interaction strength $J$ is constant. At the same time, the impact of quantum fluctuation is also considered. It is shown that good qualitative agreement is achieved with the former results [1,2]. But for small $\Delta T$ regions, where the quantum fluctuation effect is obvious, the offsets still toughly exist, which can be seen from the inserted local magnified figure.

In Fig. 5 the ferroelectric distortion inside due to the temperature gradient is considered ($J$ is variable), and the result is shown as the solid line. Comparing with the result when the ferroelectric distortion is ignored ($J$ is constant), which is shown as the dashed line, we can see that the variation of polarization offset with temperature difference is somewhat changed, especially when $\Delta T$ is small. The peak values of charge offsets shift to larger temperature difference region. When $\Delta T$ is small, the dashed charge offsets are very distinct from the background, but the solid charge offsets are not very much distinguishable. When the distortion is ignored, the uniform temperature gradient is the only factor responsible for the charge offsets. However, when the distortion is considered, both the temperature gradient and ferroelectric distortion are responsible for the charge offsets, which reflects more
realistic situation in the sample. From the nature of the distortion we have pre-articulated, it can be easily accepted that small temperature gradients lead to small distortions, and followed by the small charge offsets. Hence, the ferroelectric distortion cannot be ignored, especially when the temperature gradient is not very large, which associated with the obvious change for tiny charge offsets. It is also indicated that the absolute values of charge offsets at small $\Delta T$ regions have greatly decreased, but still exist. From this aspect this problem needs to be further explored.

In Fig. 6, the ferroelectric distortions combined with the effect of quantum fluctuation are considered at the same time. It obviously can be seen that when the quantum fluctuation is properly proposed, the charge offsets become indistinguishable from the background, which is in excellent qualitative agreement with the experimental results [1]. Quantum fluctuation effects are active when temperatures are low. With the increasing of the strength of the quantum fluctuation, the charge offsets diminish nearly to zero. Hence we can draw the conclusion that both ferroelectric distortion and quantum fluctuation effect are the two important factors to influence the formation of polarization offsets.

It should be noted that our results do not, however, completely qualitatively replicate the shape of the observed polarization offset curve in experiment, which may be explained by the fact that the model we adopted does not capture the full complexity of the ferroelectric material.

Conclusions

Polarization offset phenomena in temperature-graded ferroelectric material is investigated by means of a transverse Ising model. A function of two-spin exchange interaction strength has been introduced to describe the ferroelectric distortion due to the distribution of temperature gradients in materials. The results have shown that ferroelectric distortion and the quantum fluctuation effect are the two important factors influencing the formation of polarization offsets. Our results qualitatively agreed with the experimental observations. Especially, we have successfully replicated the indistinguishable charge offsets at low temperature gradients, which were not successfully reproduced in former theoretical studies.

Acknowledgements

This work was supported by the National Science Foundation of China under Grant No. 11374215 and the Educational Scientific Research Project of Liaoning Province under Grant No. L2014172.

References
